# Research Report (September, 2021- September, 2022)

Enrollment from September 2021

Department of Pure and Applied Mathematics

Riku Suda

### I. List of Papers

1. Riku Suda, Two Types of Solutions for A Kirchhoff Elliptic Equation with Large Growth Non-Locality and Its Singular Perturbation Problem, preprint.

#### II. List of Talks

1. "On two solutions of a Kirchhoff-type elliptic problem with high-growth non-locality", 第2回 非線形 PDE 若手ワークショップ (Online), 2022-03-15.

## III. Research Results in AY2021

Reviewing and refining the argument of ongoing research about the variational analysis on a non-local elliptic partial differential equation called "Kirchhoff-type":

$$\left\{egin{aligned} &-M\Big(\|
abla u\|_{L^2(\mathbb{R}^N)}^2\Big)\,\Delta u=g(u);\ &u\in H^1(\mathbb{R}^N)\setminus\{0\} \end{aligned}
ight.$$

Here, we assume that  $N\geq 3$ , M(s) is a positive increasing function such as  $M(s)=a+bs^{\beta}$  (s>0) with  $a,b,\beta>0$  and g represents a certain type of general non-linearity known for papers by Berestycki and Lions. More specifically, the large  $\beta$  situation is the target, which implies stronger effects from the non-local term represented by the function M.

This year, the argument has been successfully strengthened, which has enabled us to deal with more general settings.

In addition, a result for the related singularly perturbed problem:

$$-arepsilon^2 \left[ a + b \left( arepsilon^{2-N} \int_{\mathbb{R}^N} |
abla u|^2 dx 
ight)^eta 
ight] \Delta u = -V(x) u + f(u) \quad (arepsilon > 0)$$

was also obtained, which has been reviewed as well.

These results are already summarized as a preprint and being prepared for publishing (see List of Papers).

#### IV. Research Plan for AY2022

Further research on the Kirchhoff-type singular perturbed problem, like seeking multi-peak solutions.