# **Research Report 2017**

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# Publications

- Y. Cho, T. Ozawa Short-range scattering of Hartree type fractional NLS II, Nonlinear Analysis, 157(2017), 62-75. DOI:10.1016/j.na.2017.03.005
- S. Machihara, T. Ozawa, H. Wadade Remarks on the Rellich inequality, Math.Z., 286(2017), 1367-1373. DOI:10.1007/s00209-016-1805-8
- J. Fan, T. Ozawa Uniform existence and uniqueness for a time-dependent Ginzburg-Landau model for superconductivity, Nonlinear Analysis and Differential Equations, 5(2017), no.6, 249-259. https://doi.org/10.12988/nade.2017.7713
- J. Fan, T. Ozawa Local well-posedness for an Ericksen-Leslie's parabolic-hyperbolic compressible non-isothermal model for liquid crystals, Electron. J. Differential Equations, **2017**(2017), No. 232, 1-8. (Open Access)
- K. Fujiwara, T. Ozawa Lifespan of strong solutions to the periodic nonlinear Schrödinger equation without gauge invariance, Journal of Evolution Equations, 17(2017), 1023-1030.
- J. Bellazzini, T. Ozawa, N. Visciglia Ground states for semi-relativistic Schrödinger-Poisson-Slater energy, Funkcialaj Ekvacioj, 60(2017), 353-369.
- Y. Cho, G. Hwang, T. Ozawa On the focusing energy-critical fractional nonlinear Schrödinger equations, Adv. Differential Equations, 23, No.3-4, (2018), 161-192.
- Y. Cho, T. Ozawa Small data scattering of Hartree type fractional Schrödinger equations in dimension 2 and 3, J. Korean Math. Soc., 55 (2018), No.2, 373-390. https://doi.org/10.4134/JKMS.j170224

### **Invited Talks**

 "Lifespan of periodic solutions to nonlinear Schrödinger equations" RIMS Workshop Nonlinear Wave and Dispersive Equations August 30, 2017 Kyoto University, Kyoto, Japan

- "Blowup solutions for the derivative nonlinear Schrödinger equation on torus" Recent topics on PDEs November 17, 2017 Chuo University, Tokyo, Japan
- "Lifespan of periodic solutions to derivative nonlinear Schrödinger equations" Nonlinear Dispersive Equations in Kumamoto, 2018 January 20, 2018 Kumamoto University, Kumamoto, Japan
- "Lifespan of blowup solutions to the nonlinear Schrödinger equations on torus" Hyperbolic Partial Differential Equations and Related Topics-in honor of the 60th birthday of Professor Tokio Matsuyama-January 27, 2018 Chuo University, Tokyo, Japan
- "On improved Hardy inequalities" Workshop on Harmonic analysis and Nonlinear Evolution Equations February 23, 2018 Aula Magna and Sala Seminari, Department of Mathematics, Pisa, Italy

#### **Conference Organized**

1. Nonlinear Science Colloquium Waseda University

> May 31, 2017 Hiraku Nishimori (Hiroshima University) "Intelligent Group Behavior by Unintelligent Individuals: Autonomous Task Allocation Dynamics of Foraging Ants" June 29, 2017 Hideo Kozono (Waseda University) "Liouville type theorem for the Navier-Stokes equations" July 12, 2017 Hiroshi Kori (Ochanomizu University) 「体内時計をめぐる数理と実験の協働」(in Japanese)

- International Workshop on "Fundamental Problems in Mathematical and Theoretical Physics" Top Global University Project, Waseda University July 24-28, 2017
  O2 Conference Room, 1st Floor, 55 Bldg. Waseda University
- The 42st Sapporo Symposium on Partial Differential Equations August 8-10, 2017 Hokkaido University
- Workshop on Hyperbolic and Parabolic Systems December 12, 2017 Wasdea University

# **Research Summary**

- We have clarified a relationship between non-gauge structure and blowup of solutions for nonlinear Schrödinger equations.
- We have proved the existence of ground and scattering states for semirelativistic fields.
- We have formulated Rellich's inequality in the framework of equalities.